Computer-aided Harmonic Progression Analysis: CAT CaSe

Authors: Carmine Cataldo, Luigi Serra
Submitted: 6. October 2018
Published: 8. October 2018
Volume: 5
Issue: 8
Affiliation: Independent Researcher, PhD in Mechanical Engineering, MD in Disciplines of Jazz and Improvisation (Jazz Piano), Battipaglia (SA), Italy
Languages: English
Keywords: CAT CaSe, Android, Cataldo Advanced Transformations, Chord Progression Analysis, Harmonic Substitutions
DOI: 10.17160/josha.5.8.477

Abstract:
In this article we briefly introduce CAT CaSe. CAT CaSe is an innovative Android app, entirely based on an improved version of CAT (Cataldo Advanced Transformations), expressly meant for musicians (professionals and students). The app allows to instantly carry out a detailed analysis of any harmonic progression, without any exception whatsoever. All the phases that constitute the analysis are shown to the user, and the Harmonic Substitutions that occur are accurately discussed.
Computer-aided Harmonic Progression Analysis: CAT CaSe

Carmine Cataldo*, Luigi Serra**
* PhD in Mechanical Engineering, MD in Disciplines of Jazz and Improvisation – Jazz Piano, Battipaglia (SA), Italy
** R. A., ISISLab, Department of Computer Science, University of Salerno (Italy)

Abstract

In this article we briefly introduce CAT CaSe. CAT CaSe is an innovative Android app, entirely based on an improved version of CAT (Cataldo Advanced Transformations), expressly meant for musicians (professionals and students). The app allows to instantly carry out a detailed analysis of any harmonic progression, without any exception whatsoever. All the phases that constitute the analysis are shown to the user, and the Harmonic Substitutions that occur are accurately discussed.

Keywords

CAT CaSe, Android, Cataldo Advanced Transformations, Chord Progression Analysis, Harmonic Substitutions.

CAT CaSe

CAT CaSe [https://play.google.com/store/apps/details?id=serra.cataldo.catcase] is an innovative Android application (developed by Carmine Cataldo e Luigi Serra), entirely based on an improved version of CAT (Cataldo Advanced Transformations) [1], expressly meant for musicians (professionals and students). The app allows to instantly carry out a detailed analysis of any harmonic progression, without any exception whatsoever. All the phases that constitute the analysis are shown to the user, and the Harmonic Substitutions that occur are accurately discussed. For instance, every time the app resorts to the so-called "Modal Interchange", the scales between which the parallelism is set are revealed (CAT CaSe can compare up to 35 scales/modes), highlighting the degrees which are involved.

CAT CaSe, moreover, can recognize and contextualize possible "Harmonic Enrichments", such as "Tonicizations" and "Expansions" (half-cadences arisen from a single Dominant Seventh Chord). [2] [3] [4] [5]

CAT CaSe is provided with a didactic section, finalized to rigorously defining all the Harmonic Substitutions and the Enrichments.
The writing of harmonic progressions is extremely simple and incredibly fast, thanks to the introduction of an innovative interface that allows the user to completely avoid the usage of the alphanumeric keypad. For this reason, CAT CaSe turns out to be very useful during live performances, especially if it is necessary to quickly and comprehensively write, by exploiting an Android device (smartphone or tablet), a harmonic progression the musician must abide to during the accompaniment or the improvisation.

After the analysis, CAT CaSe allows the user to examine an "inverse procedure", particularly dedicated to musicians interested in composing and arranging. In a few words, starting from the final outcome of the analysis (very often, a sequence of plagal and/or perfect cadences) [4] [5], the app returns, step by step, the initial progression. As a useful additional feature, on the first page of the inverse procedure the parametric version (regardless of the particular key) of the final outcome is also shown.

The time signature must always be imagined as being equal to 4/4. For example, even if we deal with a 3/4, we have to consider four pulses per measure (four beats per bar): each beat, in this case, will be characterized by a duration equivalent to a dotted quaver.
CAT (Cataldo Advanced Transformations): Short Overview

*CAT CaSe* is entirely based on an improved version of *CAT* (Cataldo Advanced Transformations). A considerable improvement of *CAT* has been achieved by conducting an extremely thorough analysis of a huge amount of LEGO Bricks (public domain harmonic patterns) [6] [7]. Unlike the previous one [8] [9], the ultimate version of *CAT* [1] has no limitation concerning the key (any song written in both major and minor key can be analysed), exploits a more rigorous definition of “Similitude”, and takes into consideration “Modal Interchange” and “Tonicization”.

Examples

Example #1 (Major Key): “Inner Urge” (Joe Henderson) – last 8 bars

1. INITIAL STRUCTURE and HARMONIZATION VECTOR

   Harmonization Vector – The vector whose components represent the seventh chords that arise from the harmonization of the scale (in this case, the Ionian of F) [10] [11].

2. STRUCTURE REDUCTION

   Structure Reduction – Without “Structure Reduction” a correct application of *CAT* (Cataldo Advanced Transformations) is de facto impossible. Very simply, the number of bars and the duration of the chords are iteratively halved. The procedure is stopped the moment in which even a single chord characterized by a duration equal to a beat appears. “Structure Reduction” is applied every time it is possible, so as to obtain the highest simplification level [1] [8] [9].

3. STRUCTURE REDUCTION

   *See point 2 for the definition of Structure Reduction*
4. Inverse Substitutions (Modal Interchange*) involving MAJOR SEVENTH CHORDS different from $h_1$ and $h_4$

Modal Interchange – Two chords that arise from the harmonization of two different scales characterized by the same tonic (generic parallel keys) are interchangeable if they are placed in the same position (if they represent the same harmonic degree) [1] [4] [5].

**Bar Substitutions**

- **Tritone Substitution** – Any Dominant Seventh Chord, especially if altered, can be replaced, even if it were to arise from a previous harmonic substitution, by a chord of the same kind (a Dominant Seventh Chord) distant three whole tones from the initial chord [1] [2] [3] [4] [5] [8] [9].
6. SECONDARY DOMINANTS Inverse Substitutions

Secondary Dominant Substitution – Any chord, even if it were to arise from a previous harmonic substitution, can be converted into a Dominant Seventh Chord $[1][2][3][4][5][8][9]$.

7. (Inverse) DIATONIC Substitutions involving $h_6$

Diatonic Substitution – Two chords that arise from the harmonization of the same scale are interchangeable if the distance between them (between the roots) is equal to a diatonic third (both ascending and descending) $[1][2][3][4][5][8][9]$.

8. (Inverse) DIATONIC Substitutions involving $h_3$

*See point 7 for the definition of Diatonic Substitution

9. (Inverse) DIATONIC Substitutions involving $h_7$

*See point 7 for the definition of Diatonic Substitution
10. (Inverse) DIATONIC Substitutions involving $h_2$ and $h_4$  
*See point 7 for the definition of Diatonic Substitution

11. CONTRACTION (Inverse EXPANSION)  
Expansion – Any Dominant Seventh Chord, by forgoing half of its duration, can be imagined as being preceded by a Minor Seventh or a Half-Diminished Chord distant a descending perfect fourth and characterized by a duration equal to half of the one of the initial chord. In other terms, any Dominant Seventh Chord can be converted into a half-cadence [1] [2] [3] [8] [9].

12. STRUCTURE REDUCTION  
*See point 2 for the definition of Structure Reduction

13. FINAL OUTCOME
Example #2 (Minor Key): “Lullaby of Birdland” (George Shearing) – first 8 bars

1. INITIAL STRUCTURE and HARMONIZATION VECTOR

   **Harmonization Vector** – The vector whose components represent the seventh chords that arise from the harmonization of the scale (in this case, the *Aeolian* of *F*) [10][11].

   **Initial Progression**

   \[ F_7, D_7, C, F_7, B_7, E_7 \]

   - 1/12

2. STRUCTURE REDUCTION

   **Structure Reduction** – Without “Structure Reduction” a correct application of CAT (Cataldo Advanced Transformations) is de facto impossible. Very simply, the number of bars and the duration of the chords are iteratively halved. The procedure is stopped the moment in which even a single chord characterized by a duration equal to a beat appears. “Structure Reduction” is applied every time it is possible, so as to obtain the highest simplification level [1][8][9].

   **Structure Reduction**

   \[ F_7, D_7, G, C, F_7, B_7, E_7, A_7, G, C \]

   - 2/12

3. CONTRACTION (Inverse EXPANSION)

   **Expansion** – Any Dominant Seventh Chord, by forgoing half of its duration, can be imagined as being preceded by a Minor Seventh or a Half-Diminished Chord distant a descending perfect fourth and characterized by a duration equal to half of the one of the initial chord. In other terms, any Dominant Seventh Chord can be converted into a half-cadence [1][2][3][8][9].

   **Contractions (Inverse Expansion Substitutions)**

   \[ F_7, D_7, G, C, F_7, B_7, E_7, A_7, G, C \]

   - 3/12

4. Inverse Substitutions (Modal Interchange) involving HALF – DIMINISHED CHORDS different from *h₂*

   **Modal Interchange** – Two chords that arise from the harmonization of two different scales characterized by the same tonic (generic parallel keys) are interchangeable if they are placed in the same position (if they represent the same harmonic degree) [1][4][5].

   **Inverse Substitutions (Modal Interchange)**

   \[ F_7, D_7, G, C, F_7, B_7, E_7, A_7, G, C \]

   - 4/12

   **Bar Substitutions**

   - 6° F Dorian

   **mod.int.**

   - 6° F Aeolian
5. SECONDARY DOMINANTS Inverse Substitutions

Secondary Dominant Substitution – Any chord, even if it were to arise from a previous harmonic substitution, can be converted into a Dominant Seventh Chord [1] [2] [3] [4] [5] [8] [9].

6. CONTRACTION (Inverse EXPANSION)

*See point 3 for the definition of Contraction

7. (Inverse) DIATONIC Substitutions involving $h_6$

Diatonic Substitution – Two chords that arise from the harmonization of the same scale are interchangeable if the distance between them (between the roots) is equal to a diatonic third (both ascending and descending [1] [2] [3] [4] [5] [8] [9].

8. (Inverse) DIATONIC Substitutions involving $h_3$

*See point 7 for the definition of Diatonic Substitution
9. (Inverse) DIATONIC Substitutions involving $h_7$
*See point 7 for the definition of Diatonic Substitution

10. STRUCTURE REDUCTION
*See point 2 for the definition of Structure Reduction

11. Further SECONDARY DOMINANT Inverse Substitutions
*See point 5 for the definition of Secondary Dom. Substitutions

12. FINAL OUTCOME
**Inverse Procedure**

It's worth underlining how the chord progression analysis has almost nothing to do with the improvisation built on the original structure. More precisely, net of a certain "Horizontalization" the musician can exploit in facing specific harmonic aggregates, such as "Tonicizations" and "Turnarounds", the improvisation should be carried out "vertically", abiding by the local harmony.

The Local Tonal Centre can be characterized by significant fluctuations: sometimes, it is very difficult to correctly identify it, in particular when a progression cannot be regarded as manifestly "tonal" (built on cadences). And especially in this case, paradoxically, the musician should improvise by abiding by the harmonic progression, chord by chord [12 – 29].
References


